Calculation Policy

Mathematics is an interconnected subject in which pupils need to be able to move fluently between representations of mathematical ideas. The programmes of study are, by necessity, organised into apparently distinct domains, but pupils should make rich connections across mathematical ideas to develop fluency, mathematical reasoning and competence in solving increasingly sophisticated problems. They should also apply their mathematical knowledge to science and other subjects.

## National Curriculum 2014

## Aims

The national curriculum for mathematics aims to ensure that all pupils:

- become fluent in the fundamentals of mathematics, including through varied and frequent practice with increasingly complex problems over time, so that pupils develop conceptual understanding and the ability to recall and apply knowledge rapidly and accurately.
- reason mathematically by following a line of enquiry, conjecturing relationships and generalisations, and developing an argument, justification or proof using mathematical language.
- can solve problems by applying their mathematics to a variety of routine and non-routine problems with increasing sophistication, including breaking down problems into a series of simpler steps and persevering in seeking solutions.


## Calculation Policy

Our policy is broken down into the four operations: addition, subtraction, multiplication and division.
At the start of each area, there is an overview of the different models and images that we use to support the teaching of each concept. It is understood that many of these models are transferable, used across all areas of the teaching and learning of Maths.
Each operation is then broken down into skills, with each skill being explored in a greater depth with the different models and images that could be used to effectively teach that concept.
At the end of the policy there is a glossary of terms to support understanding of the key language used to teach the four operations.

## Introduction

A sound understanding of the number system is essential for children to carry out calculations efficiently and accurately.
Written methods of calculations are based on mental strategies. Each of the four operations builds on mental skills which provide the foundation for jottings and informal written methods of recording. Skills need to be taught, practised and reviewed constantly.
When teaching a new strategy it is important to start with numbers that the pupil can easily manipulate so that they can understand the methodology. The methods we use are in line with the teaching and learning approach by White Rose Maths, the scheme of learning we implement as a school.
The transition between stages should not be hurried as not all children will be ready to move on to the next stage at the same time, therefore the progression in this document is outlined in stages. Previous stages may need to be revisited to consolidate understanding when introducing a new strategy.
The quality and variety of mathematical vocabulary pupils hear and speak are key factors in developing their mathematical justification, argument and proof. They must be assisted in making their thinking clear to themselves as well as others. Teachers should ensure that pupils build secure foundations by using discussion to probe and remedy their misconceptions.

## Structuring Learning

It should not be forgotten that pupils require a range of different model to help them grasp new concept, embed understanding and apply it to a range of situations.
Therefore, we apply 3 main structures of learning which are interchangeable and should be used every area of Maths for all age groups.


Concrete


Pictorial

$$
15+7=22
$$

$15 \times 6=90$

## Facilitating Learning

## Concrete

Pupils should have access to a range of suitable manipulatives so that they can explore concepts in ways that make sense to them.

## Pictorial

Pupils should explore how they can record their concrete representatives in a way that they understand.

## Abstract

Pupils use their own written or mental strategies that do not rely on a visual representation.

It is important for children to see calculations written in different ways. They must understand that ' $=$ ' is 'equal to' and can appear in different places in a number sentence.

## Part-Whole Model



## Benefits

This part-whole model supports children in their understanding of aggregation and partitioning. Due to its shape, it can be referred to as a cherry part-whole model.

When the parts are complete and the whole is empty, children use aggregation to add the parts together to find the total.

When the whole is complete and at least one of the parts is empty, children use partitioning (a form of subtraction) to find the missing part.

Part-whole models can be used to partition a number into two or more parts, or to help children to partition a number into tens and ones or other place value columns.

In KS2, children can apply their understanding of the part-whole model to add and subtract fractions, decimals and percentages.

## Bar Model (single)



## Benefits

The single bar model is another type of a part-whole model that can support children in representing calculations to help them unpick the structure.

Cubes and counters can be used in a line as a concrete representation of the bar model.

Discrete bar models are a good starting point with smaller numbers. Each box represents one whole.

The combination bar model can support children to calculate by counting on from the larger number. It is a good stepping stone towards the continuous bar model.

Continuous bar models are useful for a range of values. Each rectangle represents a number. The question mark indicates the value to be found.

In KS2, children can use bar models to represent larger numbers, decimals and fractions.

## Bar Model



## Benefits

Children can use the single bar model to represent multiplication as repeated addition. They could use counters, cubes or dots within the bar model to support calculation before moving on to placing digits into the bar model to represent the multiplication.

Division can be represented by showing the total of the bar model and then dividing the bar model into equal groups.

It is important when solving word problems that the bar model represents the problem.

Sometimes, children may look at scaling problems. In this case, more than one bar model is useful to represent this type of problem, e.g. There are 3 girls in a group. There are 5 times more boys than girls. How many boys are there?
The multiple bar model provides an opportunity to compare the groups.

## Bar Model (multiple)

## Discrete



$$
7+3=10
$$



Continuous
$\square$


$7-3=4$

$$
7-3=4
$$

$2,394-1,014=1,380$

## Benefits

The multiple bar model is a good way to compare quantities whilst still unpicking the structure.

Two or more bars can be drawn, with a bracket labelling the whole positioned on the right hand side of the bars. Smaller numbers can be represented with a discrete bar model whilst continuous bar models are more effective for larger numbers.

Multiple bar models can also be used to represent the difference in subtraction. An arrow can be used to model the difference.

When working with smaller numbers, children can use cubes and a discrete model to find the difference. This supports children to see how counting on can help when finding the difference.

## Number Shapes



## Benefits

Number shapes can be useful to support children to subitise numbers as well as explore aggregation, partitioning and number bonds.

When adding numbers, children can see how the parts come together making a whole. As children use number shapes more often, they can start to subitise the total due to their familiarity with the shape of each number.

When subtracting numbers, children can start with the whole and then place one of the parts on top of the whole to see what part is missing. Again, children will start to be able to subitise the part that is missing due to their familiarity with the shapes.

Children can also work systematically to find number bonds. As they increase one number by 1 , they can see that the other number decreases by 1 to find all the possible number bonds for a number.

## Number Shapes


$18 \div 3=6$

## Benefits

Number shapes support children's understanding of multiplication as repeated addition.

Children can build multiplications in a row using the number shapes. When using odd numbers, encourage children to interlock the shapes so there are no gaps in the row. They can then use the tens number shapes along with other necessary shapes over the top of the row to check the total. Using the number shapes in multiplication can support children in discovering patterns of multiplication e.g. odd $\mathbf{x}$ odd $=$ even, odd $\mathbf{x}$ even $\boldsymbol{=}$ odd, even $\boldsymbol{x}$ even $\boldsymbol{=}$ even.

When dividing, number shapes support children's understanding of division as grouping. Children make the number they are dividing and then place the number shape they are dividing by over the top of the number to find how many groups of the number there are altogether e.g. There are 6 groups of 3 in 18 .

## Cubes



## Benefits

Cubes can be useful to support children with the addition and subtraction of one-digit numbers.

When adding numbers, children can see how the parts come together to make a whole. Children could use two different colours of cubes to represent the numbers before putting them together to create the whole.

When subtracting numbers, children can start with the whole and then remove the number of cubes that they are subtracting in order to find the answer. This model of subtraction is reduction, or take away.

Cubes can also be useful to look at subtraction as difference. Here, both numbers are made and then lined up to find the difference between the numbers.

Cubes are useful when working with smaller numbers but are less efficient with larger numbers as they are difficult to subitise and children may miscount them.

## Ten Frames (within 10)



## Ten Frames (within 20)



10

## Benefits

When adding two single digits, children can make each number on separate ten frames before moving part of one number to make 10 on one of the ten frames. This supports children to see how they have partitioned one of the numbers to make 10, and makes links to effective mental methods of addition.

When subtracting a one-digit number from a two-digit number, firstly make the larger number on 2 ten frames. Remove the smaller number, thinking carefully about how you have partitioned the number to make 10, this supports mental methods of subtraction.

When adding three single-digit numbers, children can make each number on 3 separate 10 frames before considering which order to add the numbers in. They may be able to find a number bond to 10 which makes the calculation easier. Once again, the ten frames support the link to effective mental methods of addition as well as the importance of commutativity.

## Bead Strings

## Benefits

Different sizes of bead strings can support children at different stages of addition and subtraction.

Bead strings to 10 are very effective at helping children to investigate number bonds up to 10 .
They can help children to systematically find all the number bonds to 10 by moving one bead at a time to see the different numbers they have partitioned the 10 beads into e.g. $2+8=10$, move one bead, $3+7=10$.

Bead strings to 20 work in a similar way but they also group the beads in fives. Children can apply their knowledge of number bonds to 10 and see the links to number bonds to 20 .

Bead strings to 100 are grouped in tens and can support children in number bonds to 100 as well as helping when adding by making ten. Bead strings can show a link to adding to the next 10 on number lines which supports a mental method of addition.

## Bead Strings

$-000-000-000-000-000-$

| $5 \times 3=15$ |
| :--- |
| $3 \times 5=15$ |$\quad 15 \div 3=5$

$-00000-00000-00000-$
$5 \times 3=15 \quad 15 \div 5=3$
$3 \times 5=15 \quad$

## Benefits

Bead strings to 100 can support children in their understanding of multiplication as repeated addition. Children can build the multiplication using the beads. The colour of beads supports children in seeing how many groups of 10 they have, to calculate the total more efficiently.
Encourage children to count in multiples as they build the number e.g. 4, 8, 12, 16, 20.

Children can also use the bead string to count forwards and backwards in multiples, moving the beads as they count.

When dividing, children build the number they are dividing and then group the beads into the number they are dividing by e.g. 20 divided by 4 - Make 20 and then group the beads into groups of four. Count how many groups you have made to find the answer.

## Number Tracks



## Number Tracks



$$
\begin{aligned}
& 6 \times 3=18 \\
& 3 \times 6=18
\end{aligned}
$$



$$
18 \div 3=6
$$

## Benefits

Number tracks are useful to support children to count in multiples, forwards and backwards. Moving counters or cubes along the number track can support children to keep track of their counting. Translucent counters help children to see the number they have landed on whilst counting.

When multiplying, children place their counter on 0 to start and then count on to find the product of the numbers.
When dividing, children place their counter on the number they are dividing and the count back in jumps of the number they are dividing by until they reach 0 . Children record how many jumps they have made to find the answer to the division.

Number tracks can be useful with smaller multiples but when reaching larger numbers they can become less efficient.

## Number Lines (labelled)


$14-6=8$


## Benefits

Labelled number lines support children in their understanding of addition and subtraction as augmentation and reduction.

Children can start by counting on or back in ones, up or down the number line. This skill links directly to the use of the number track.

Progressing further, children can add numbers by jumping to the nearest 10 and then jumping to the total. This links to the making 10 method which can also be supported by ten frames. The smaller number is partitioned to support children to make a number bond to 10 and to then add on the remaining part.

Children can subtract numbers by firstly jumping to the nearest 10. Again, this can be supported by ten frames so children can see how they partition the smaller number into the two separate jumps.

## Number Lines (labelled)



## Benefits

Labelled number lines are useful to support children to count in multiples, forwards and backwards as well as calculating single-digit multiplications.

When multiplying, children start at 0 and then count on to find the product of the numbers.
When dividing, start at the number they are dividing and the count back in jumps of the number they are dividing by until they reach 0 .
Children record how many jumps they have made to find the answer to the division.

Labelled number lines can be useful with smaller multiples, however they become inefficient as numbers become larger due to the required size of the number line.

## Number Lines (blank)

$35+37=72$

$35+37=72$


$$
72-35=37
$$



## Benefits

Blank number lines provide children with a structure to add and subtract numbers in smaller parts.

Developing from labelled number lines, children can add by jumping to the nearest 10 and then adding the rest of the number either as a whole or by adding the tens and ones separately.

Children may also count back on a number line to subtract, again by jumping to the nearest 10 and then subtracting the rest of the number.

Blank number lines can also be used effectively to help children subtract by finding the difference between numbers. This can be done by starting with the smaller number and then counting on to the larger number. They then add up the parts they have counted on to find the difference between the numbers.

## Number Lines (blank)

## Benefits

Children can use blank number lines to represent scaling as multiplication or division.

Blank number lines with intervals can support children to represent scaling accurately. Children can label intervals with multiples to calculate scaling problems.

Blank number lines without intervals can also be used for children to represent scaling.

## Straws



## Benefits

Straws are an effective way to support children in their understanding of exchange when adding and subtracting 2-digit numbers.

Children can be introduced to the idea of bundling groups of ten when adding smaller numbers and when representing 2 -digit numbers. Use elastic bands or other ties to make bundles of ten straws.

When adding numbers, children bundle a group of 10 straws to represent the exchange from 10 ones to 1 ten. They then add the individual straws (ones) and bundles of straws (tens) to find the total.

When subtracting numbers, children unbundle a group of 10 straws to represent the exchange from 1 ten to 10 ones.

Straws provide a good stepping stone to adding and subtracting with Base 10/Dienes.

## Base 10/Dienes (addition)



38


1


265 + 164


1

## Benefits

Using Base 10 or Dienes is an effective way to support children's understanding of column addition. It is important that children write out their calculations alongside using or drawing Base 10 so they can see the clear links between the written method and the model.

Children should first add without an exchange before moving on to addition with exchange.. The representation becomes less efficient with larger numbers due to the size of Base 10. In this case, place value counters may be the better model to use.

When adding, always start with the smallest place value column. Here are some questions to support children. How many ones are there altogether?
Can we make an exchange? (Yes or No)
How many do we exchange? ( 10 ones for 1 ten, show exchanged 10 in tens column by writing 1 in column) How many ones do we have left? (Write in ones column) Repeat for each column.

## Base 10/Dienes (subtraction)



## Benefits

Using Base 10 or Dienes is an effective way to support children's understanding of column subtraction. It is important that children write out their calculations alongside using or drawing Base 10 so they can see the clear links between the written method and the model.

Children should first subtract without an exchange before moving on to subtraction with exchange. When building the model, children should just make the minuend using Base 10, they then subtract the subtrahend. Highlight this difference to addition to avoid errors by making both numbers. Children start with the smallest place value column. When there are not enough
ones/tens/hundreds to subtract in a column, children need to move to the column to the left and exchange e.g. exchange 1 ten for 10 ones. They can then subtract efficiently.
This model is efficient with up to 4-digit numbers. Place value counters are more efficient with larger numbers and decimals.

## Base 10/Dienes (multiplication)



## Benefits

Using Base 10 or Dienes is an effective way to support children's understanding of column multiplication. It is important that children write out their calculation alongside the equipment so they can see how the concrete and written representations match.

As numbers become larger in multiplication or the amounts of groups becomes higher, Base 10 / Dienes becomes less efficient due to the amount of equipment and number of exchanges needed.

Base 10 also supports the area model of multiplication well. Children use the equipment to build the number in a rectangular shape which they then find the area of by calculating the total value of the pieces This area model can be linked to the grid method or the formal column method of multiplying 2-digits by 2 -digits.

## Base 10/Dienes (division)



## Benefits

Using Base 10 or Dienes is an effective way to support children's understanding of division.

When numbers become larger, it can be an effective way to move children from representing numbers as ones towards representing them as tens and ones in order to divide. Children can then share the Base 10/ Dienes between different groups e.g. by drawing circles or by rows on a place value grid.

When they are sharing, children start with the larger place value and work from left to right. If there are any left in a column, they exchange e.g. one ten for ten ones. When recording, encourage children to use the partwhole model so they can consider how the number has been partitioned in order to divide. This will support them with mental methods.

## Place Value Counters (addition)



384
$+237$ 621

11

3.65


## Benefits

Using place value counters is an effective way to support children's understanding of column addition. It is important that children write out their calculations alongside using or drawing counters so they can see the clear links between the written method and the model.

Children should first add without an exchange before moving on to addition with exchange. Different place value counters can be used to represent larger numbers or decimals. If you don't have place value counters, use normal counters on a place value grid to enable children to experience the exchange between columns.

When adding money, children can also use coins to support their understanding. It is important that children consider how the coins link to the written calculation especially when adding decimal amounts.

## Place Value Counters (Subtraction)



## Benefits

Using place value counters is an effective way to support children's understanding of column subtraction. It is important that children write out their calculations alongside using or drawing counters so they can see the clear links between the written method and the model.

Children should first subtract without an exchange before moving on to subtraction with exchange. If you don't have place value counters, use normal counters on a place value grid to enable children to experience the exchange between columns.

When building the model, children should just make the minuend using counters, they then subtract the subtrahend. Children start with the smallest place value column. When there are not enough ones/tens/hundreds to subtract in a column, children need to move to the column to the left and exchange e.g. exchange 1 ten for 10 ones. They can then subtract efficiently.

## Place Value Counters (multiplication)



## Benefits

Using place value counters is an effective way to support children's understanding of column multiplication. It is important that children write out their calculation alongside the equipment so they can see how the concrete and written match.

As numbers become larger in multiplication or the amounts of groups becomes higher, Base 10 / Dienes becomes less efficient due to the amount of equipment and number of exchanges needed The counters should be used to support the understanding of the written method rather than support the arithmetic.

Place value counters also support the area model of multiplication well. Children can see how to multiply 2digit numbers by 2-digit numbers.

## Place Value Counters (division)



1223
$4489{ }^{1}$

## Benefits

Using place value counters is an effective way to support children's understanding of division.

When working with smaller numbers, children can use place value counters to share between groups. They start by sharing the larger place value column and work from left to right. If there are any counters left over once they have been shared, they exchange the counter e.g. exchange one ten for ten ones. This method can be linked to the part-whole model to support children to show their thinking.

Place value counters also support children's understanding of short division by grouping the counters rather than sharing them. Children work from left to right through the place value columns and group the counters in the number they are dividing by. If there are any counters left over after they have been grouped, they exchange the counter e.g. exchange one hundred for ten tens.

## Addition

| Skill | Years | Representations and Models |  |
| :---: | :---: | :---: | :---: |
| Add two 1-digit <br> numbers to 10 | 1 | Part-whole model <br> Bar model <br> Number shapes | Ten frames (within 10) <br> Bead strings (10) <br> Number tracks |
| Add 1 and 2-digit <br> numbers to 20 | $1 / 2$ | Part-whole model <br> Bar model <br> Number shapes <br> Ten frames (within 20) | Bead strings (10) <br> Number tracks <br> Number lines (labelled) <br> Straws |
| Add three 1-digit <br> numbers | 2 | Part-whole model <br> Bar model | Ten frames (within 20) <br> Number shapes |
| Add 1 and 2-digit <br> numbers to 100 | $2 / 3$ | Part-whole model <br> Bar model <br> Number lines (labelled) | Number lines (blank) <br> Straws <br> Hundred square |
| Add two 2-digit <br> numbers | $2 / 3$ | Part-whole model <br> Bar model | Place value counters <br> Column addition |

## Addition

| Skill | Years | Representations and Models |  |
| :---: | :---: | :---: | :---: |
| Add with up to 3- <br> digits | 3 | Part-whole model <br> Bar model | Base 10 <br> Place value counters <br> Column addition |
| Add with up to 4- <br> digits | 4 | Part-whole model <br> Bar model | Base 10 <br> Place value counters <br> Column addition |
| Add with more than <br> $4^{- \text {digits }}$ | $5 / 6$ | Part-whole model <br> Bar model | Place value counters <br> Column addition |
| Add with up to 3 <br> decimal places | 5 | Part-whole model <br> Bar model | Place value counters <br> Column addition |

Skill: Add 1-digit numbers within 10 Year: 10


Skill: Add three 1-digit numbers $\quad$| Year: 2 |
| :--- |



| Skill: Add two 2-digit numbers to 100 | Year: $2 / 3$ |
| :--- | :--- |






## Subtraction

| Skill | Years | Representations and Models |  |
| :---: | :---: | :---: | :---: |
| Subtract two 1-digit <br> numbers to 10 | 1 | Part-whole model <br> Bar model <br> Number shapes | Ten frames (within 10) <br> Bead strings (10) <br> Number tracks |
| Subtract 1 and 2- <br> digit numbers to 20 | $1 / 2$ | Part-whole model <br> Bar model <br> Number shapes <br> Ten frames (within 20) | Bead strings (10) <br> Number tracks <br> Number lines (labelled) <br> Straws |
| Subtract 1 and 2- <br> digit numbers to 100 | 2 | Part-whole model <br> Bar model <br> Number lines (labelled) | Number lines (blank) <br> Straws |
| Subtract two 2-digit <br> numbers | 2 | Part-whole model <br> Bar model <br> Number lines (blank) <br> Straws | Base 10 <br> Place value counters <br> Column subtraction |

## Subtraction

| Skill | Years | Representations and Models |  |
| :---: | :---: | :---: | :---: |
| Subtract with up to <br> 3-digit | 3 | Part-whole model <br> Bar model | Base 10 <br> Place value counters <br> Column subtraction |
| Subtract with up to <br> 4-digits | 4 | Part-whole model <br> Bar model | Base 10 <br> Place value counters <br> Column subtraction |
| Subtract with more <br> than 4 digits | $5 / 6$ | Part-whole model <br> Bar model | Place value counters <br> Column subtraction |
| Subtract with up to <br> 3 decimal places | 5 | Part-whole model <br> Bar model | Place value counters <br> Column subtraction |




| Skill: Subtract 1 and 2-digit numbers to 100 | Year: 2 |
| :---: | :---: |
|  | At this stage, encourage children to use the formal column method when calculating alongside straws, base 10 or place value counters. As numbers become larger, straws become less efficient. <br> Children can also use a blank number line to count on to find the difference. Encourage them to jump to multiples of 10 to become more efficient. |


| Skill: Subtract numbers with up to 3 digits |  |  |  |  |  | Year: 3 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 27 <br> 43 <br> Ones | $5-27$ $\begin{array}{r} 3 \\ 435 \\ -\quad 273 \\ \hline 262 \\ \hline \end{array}$ | $=26$ |  |  | Base 10 and place value counters are the most effective manipulative when subtracting numbers with up to 3 digits. <br> Ensure children write out their calculation alongside any concrete resources so they can see the links to the written column method. <br> Plain counters on a place value grid can also be used to support learning. |





## Times Tables

| Skill | Years | Representations and Models |  |
| :---: | :---: | :---: | :---: |
| Recall and uses <br> multiplication and <br> division facts for the <br> 2-times table. | 2 | Bar model <br> Number shapes <br> Counters <br> Money | Ten frames <br> Bead strings |
| Recall and uses <br> multiplication and <br> division facts for the <br> 5 -times table. | 2 | Number lines <br> Everyday objects |  |
| Recall and uses <br> multiplication and <br> division facts for the <br> 10-times table. | 2 | Bumber shapes <br> Counters <br> Money | Ten frames <br> Bead strings <br> Number lines |
| Recall and uses <br> multiplication and <br> division facts for the <br> 3-times table. | 3 | Hundred square <br> Number shapes <br> Counters <br> Money | Ten frames <br> Bead strings |

## Times Tables

| Skill | Years | Representations and Models |  |
| :---: | :---: | :---: | :---: |
| Recall and uses <br> multiplication and <br> division facts for the <br> 4-times table. | 3 | Hundred square <br> Number shapes <br> Counters | Bead strings <br> Number lines <br> Everyday objects |
| Recall and uses <br> multiplication and <br> division facts for the <br> 8-times table. | 3 | Hundred square <br> Number shapes <br> Counters | Bead strings <br> Number lines |
| Recall and uses <br> multiplication and <br> division facts for the <br> 6-times table. | 4 | Hundred square <br> Number shapes | Bead strings <br> Number lines |
| Recall and uses <br> multiplication and <br> division facts for the <br> 7-times table. | 4 | Hundred square |  |
| Number shapes |  |  |  |

## Times Tables

| Skill | Years | Representations and Models |  |
| :---: | :---: | :---: | :---: |
| Recall and uses <br> multiplication and <br> division facts for the <br> 9-times table. | 4 | Hundred square <br> Number shapes <br> Counters | Bead strings <br> Number lines <br> Everyday objects |
| Recall and uses <br> multiplication and <br> division facts for the <br> 11-times table. | 4 | Hundred square <br> Base 10 | Place value counters <br> Number lines |
| Recall and uses <br> multiplication and <br> division facts for the <br> 12-times table. | 4 | Hundred square <br> Base 10 | Place value counters |
| Number lines |  |  |  |



Encourage daily counting in multiples both forwards and backwards. This can be supported using a number line or a hundred square.

Look for patterns in the two times table, using concrete manipulatives to support. Notice how all the numbers are even and there is a pattern in the ones.

Use different models to develop fluency.

-00000-00000-00000-00000-


| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 |
| 21 | 22 | 23 | 24 | 25 | 26 | 27 | 28 | 29 | 30 |
| 31 | 32 | 33 | 34 | 35 | 36 | 37 | 38 | 39 | 40 |
| 41 | 42 | 43 | 44 | 45 | 46 | 47 | 48 | 49 | 50 |



## 000090000000000



| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 |
| 21 | 22 | 23 | 24 | 25 | 26 | 27 | 28 | 29 | 30 |
| 31 | 32 | 33 | 34 | 35 | 36 | 37 | 38 | 39 | 40 |
| 41 | 42 | 43 | 44 | 45 | 46 | 47 | 48 | 49 | 50 |
| 51 | 52 | 53 | 54 | 55 | 56 | 57 | 58 | 59 | 60 |
| 61 | 62 | 63 | 64 | 65 | 66 | 67 | 68 | 69 | 70 |
| 71 | 72 | 73 | 74 | 75 | 76 | 77 | 78 | 79 | 80 |
| 81 | 82 | 83 | 84 | 85 | 86 | 87 | 88 | 89 | 90 |
| 91 | 92 | 93 | 94 | 95 | 96 | 97 | 98 | 99 | 00 |

Encourage daily counting in multiples both forwards and backwards. This can be supported using a number line or a hundred square.

Look for patterns in the ten times table, using concrete manipulatives to support. Notice the pattern in the digitsthe ones are always 0 , and the tens increase by 1 ten each time.


| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 |
| 21 | 22 | 23 | 24 | 25 | 26 | 27 | 28 | 29 | 30 |
| 31 | 32 | 33 | 34 | 35 | 36 | 37 | 38 | 39 | 40 |
| 41 | 42 | 43 | 44 | 45 | 46 | 47 | 48 | 49 | 50 |



3


6


9

12


Encourage daily counting in multiples both forwards and backwards. This can be supported using a number line or a hundred square.

Look for patterns in the three times table, using concrete manipulatives to support. Notice the odd, even, odd, even pattern using number shapes to support. Highlight the pattern in the ones using a hundred square.

Skill: 4 times table


| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 |
| 21 | 22 | 23 | 24 | 25 | 26 | 27 | 28 | 29 | 30 |
| 31 | 32 | 33 | 34 | 35 | 36 | 37 | 38 | 39 | 40 |
| 41 | 42 | 43 | 44 | 45 | 46 | 47 | 48 | 49 | 50 |


| 4 | 8 | 12 | 16 | 20 |
| :---: | :---: | :---: | :---: | :---: |
| 24 | 28 | 32 | 36 | 40 |
| 44 | 48 | 52 | 56 | 60 |

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Year: 3
Encourage daily counting in multiples, supported by a number line or a hundred square. Look for patterns in the four times table, using manipulatives to support. Make links to the 2 times table, seeing how each multiple is double the twos. Notice the pattern in the ones within each group of five multiples.
Highlight that all the multiples are even using number shapes to support.

## Skill: 8 times table

Year: 3

## 



8


16


24
32

| 8 | 16 | 24 | 32 | 40 |
| :---: | :---: | :---: | :---: | :---: |
| 48 | 56 | 64 | 72 | 80 |


| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 |
| 21 | 22 | 23 | 24 | 25 | 26 | 27 | 28 | 29 | 30 |
| 31 | 32 | 33 | 34 | 35 | 36 | 37 | 38 | 39 | 40 |
| 41 | 42 | 43 | 44 | 45 | 46 | 47 | 48 | 49 | 50 |
| 51 | 52 | 53 | 54 | 55 | 56 | 57 | 58 | 59 | 60 |
| 61 | 62 | 63 | 64 | 65 | 66 | 67 | 68 | 69 | 70 |
| 71 | 72 | 73 | 74 | 75 | 76 | 77 | 78 | 79 | 80 |
| 81 | 82 | 83 | 84 | 85 | 86 | 87 | 88 | 89 | 90 |
| 91 | 92 | 93 | 94 | 95 | 96 | 97 | 98 | 99 | 100 |

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Encourage daily counting in multiples, supported by a number line or a hundred square. Look for patterns in the eight times table, using manipulatives to support. Make links to the 4 times table, seeing how each multiple is double the fours. Notice the pattern in the ones within each group of five multiples. Highlight that all the multiples are even using number shapes to support.

| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 |
| 21 | 22 | 23 | 24 | 25 | 26 | 27 | 28 | 29 | 30 |
| 31 | 32 | 33 | 34 | 35 | 36 | 37 | 38 | 39 | 40 |
| 41 | 42 | 43 | 44 | 45 | 46 | 47 | 48 | 49 | 50 |
| 51 | 52 | 53 | 54 | 55 | 56 | 57 | 58 | 59 | 60 |
| 61 | 62 | 63 | 64 | 65 | 66 | 67 | 68 | 69 | 70 |
| 71 | 72 | 73 | 74 | 75 | 76 | 77 | 78 | 79 | 80 |
| 81 | 82 | 83 | 84 | 85 | 86 | 87 | 88 | 89 | 90 |
| 91 | 92 | 93 | 94 | 95 | 96 | 97 | 98 | 99 | 100 |

Encourage daily counting in multiples， supported by a number line or a hundred square． Look for patterns in the six times table， using manipulatives to support．Make links to the 3 times table， seeing how each multiple is double the threes．Notice the pattern in the ones within each group of five multiples．
Highlight that all the multiples are even using number shapes to support．

## 

| 9 | 18 | 27 | 36 | 45 |
| :---: | :---: | :---: | :---: | :---: |
| 54 | 63 | 72 | 81 | 90 |


| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 |
| 21 | 22 | 23 | 24 | 25 | 26 | 27 | 28 | 29 | 30 |
| 31 | 32 | 33 | 34 | 35 | 36 | 37 | 38 | 39 | 40 |
| 41 | 42 | 43 | 44 | 45 | 46 | 47 | 48 | 49 | 50 |
| 51 | 52 | 53 | 54 | 55 | 56 | 57 | 58 | 59 | 60 |
| 61 | 62 | 63 | 64 | 65 | 66 | 67 | 68 | 69 | 70 |
| 71 | 72 | 73 | 74 | 75 | 76 | 77 | 78 | 79 | 80 |
| 81 | 82 | 83 | 84 | 85 | 86 | 87 | 88 | 89 | 90 |
| 91 | 92 | 93 | 94 | 95 | 96 | 97 | 98 | 99 | 100 |

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Encourage daily counting in multiples both forwards and backwards. This can be supported using a number line or a hundred square. Look for patterns in the nine times table, using concrete manipulatives to support. Notice the pattern in the tens and ones using the hundred square to support as well as noting the odd, even pattern within the multiples.


| 7 | 14 | 21 | 28 | 35 |
| :---: | :---: | :---: | :---: | :---: |
| 42 | 49 | 56 | 63 | 70 |


| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 |
| 21 | 22 | 23 | 24 | 25 | 26 | 27 | 28 | 29 | 30 |
| 31 | 32 | 33 | 34 | 35 | 36 | 37 | 38 | 39 | 40 |
| 41 | 42 | 43 | 44 | 45 | 46 | 47 | 48 | 49 | 50 |
| 51 | 52 | 53 | 54 | 55 | 56 | 57 | 58 | 59 | 60 |
| 61 | 62 | 63 | 64 | 65 | 66 | 67 | 68 | 69 | 70 |
| 71 | 72 | 73 | 74 | 75 | 76 | 77 | 78 | 79 | 80 |
| 81 | 82 | 83 | 84 | 85 | 86 | 87 | 88 | 89 | 90 |
| 91 | 92 | 93 | 94 | 95 | 96 | 97 | 98 | 99 | 100 |

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Encourage daily counting in multiples both forwards and backwards, supported by a number line or a hundred square. The seven times table can be trickier to learn due to the lack of obvious pattern in the numbers, however they already know several facts due to commutativity. Children can still see the odd, even pattern in the multiples using number shapes to support.

| 11 | 22 | 33 | 44 | 55 | 66 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 77 | 88 | 99 | 110 | 121 | 132 |



| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 |
| 21 | 22 | 23 | 24 | 25 | 26 | 27 | 28 | 29 | 30 |
| 31 | 32 | 33 | 34 | 35 | 36 | 37 | 38 | 39 | 40 |
| 41 | 42 | 43 | 44 | 45 | 46 | 47 | 48 | 49 | 50 |
| 51 | 52 | 53 | 54 | 55 | 56 | 57 | 58 | 59 | 60 |
| 61 | 62 | 63 | 64 | 65 | 66 | 67 | 68 | 69 | 70 |
| 71 | 72 | 73 | 74 | 75 | 76 | 77 | 78 | 79 | 80 |
| 81 | 82 | 83 | 84 | 85 | 86 | 87 | 88 | 89 | 90 |
| 91 | 92 | 93 | 94 | 95 | 96 | 97 | 98 | 99 | 100 |



Encourage daily counting in multiples both forwards and backwards. This can be supported using a number line or a hundred square.

Look for patterns in the eleven times table, using concrete manipulatives to support. Notice the pattern in the tens and ones using the hundred square to support. Also consider the pattern after crossing 100

| 12 | 24 | 36 | 48 | 60 |
| :---: | :---: | :---: | :---: | :---: |
| 72 | 84 | 96 | 108 | 120 |
| 132 | 144 |  |  |  |



| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 |
| 21 | 22 | 23 | 24 | 25 | 26 | 27 | 28 | 29 | 30 |
| 31 | 32 | 33 | 34 | 35 | 36 | 37 | 38 | 39 | 40 |
| 41 | 42 | 43 | 44 | 45 | 46 | 47 | 48 | 49 | 50 |
| 51 | 52 | 53 | 54 | 55 | 56 | 57 | 58 | 59 | 60 |
| 61 | 62 | 63 | 64 | 65 | 66 | 67 | 68 | 69 | 70 |
| 71 | 72 | 73 | 74 | 75 | 76 | 77 | 78 | 79 | 80 |
| 81 | 82 | 83 | 84 | 85 | 86 | 87 | 88 | 89 | 90 |
| 91 | 92 | 93 | 94 | 95 | 96 | 97 | 98 | 99 | 100 |



Encourage daily counting in multiples, supported by a number line or a hundred square. Look for patterns in the 12 times table, using manipulatives to support. Make links to the 6 times table, seeing how each multiple is double the sixes. Notice the pattern in the ones within each group of five multiples. The hundred square can support in highlighting this pattern.

## Multiplication

| Skill | Years | Representations and Models |  |
| :---: | :---: | :---: | :---: |
| Solve one-step <br> problems with <br> multiplication | $1 / 2$ | Bar model <br> Number shapes <br> Counters | Ten frames <br> Bead strings <br> Number lines |
| Multiply 2-digit by 1- <br> digit numbers | $3 / 4$ | Place value counters <br> Base 10 | Short written method <br> Expanded written method |
| Multiply 3-digit by 1- <br> digit numbers | 4 | Place value counters <br> Base 10 | Short written method |
| Multiply 4-digit by 1- <br> digit numbers | 5 | Place value counters | Short written method |
| Multiply 2-digit by <br> 2-digit numbers | 5 | Place value counters <br> Base 10 | Short written method |
| Grid method |  |  |  |$|$| Multiply 2-digit by 3- <br> digit numbers | 5 | Place value counters |
| :---: | :---: | :---: | Short written method | Grid method |
| :--- |

Skill: Solve 1-step problems using multiplication $\quad$\begin{tabular}{l}
Year: $1 / 2$ <br>

| lhildren represent |
| :--- |
| multiplication as |
| repeated addition in |
| many different ways. | <br>

In Year 1, children use <br>
concrete and pictorial <br>
representations to <br>
solve problems. They <br>
are not expected to <br>
record multiplication <br>
formally.
\end{tabular}




Skill: Multiply 2-digit numbers by 2-digit numbers



## Division

| Skill | Years | Representations and Models |  |
| :---: | :---: | :---: | :---: |
| Solve one-step <br> problems with <br> division (sharing) | $1 / 2$ | Bar model <br> Real life objects | Arrays <br> Counters |
| Solve one-step <br> problems with <br> division (grouping) | $1 / 2$ | Real life objects <br> Number shapes <br> Bead strings <br> Ten frames | Number lines <br> Arrays <br> Counters |
| Divide 2-digits by 1- <br> digit (no exchange <br> sharing) | 3 | Straws <br> Base 10 <br> Bar model | Place value counters <br> Part-whole model |
| Divide 2-digits by 1- <br> digit (sharing with <br> exchange) | 3 | Straws <br> Base 10 <br> Bar model | Place value counters |
| Divide 2-digits by 1- <br> digit (sharing with <br> remainders) | $3 / 4$ | Straws <br> Base 10 <br> Bar model | Place value counters |

## Division

| Skill | Years | Representations and Models |  |
| :---: | :---: | :---: | :---: |
| Divide 2-digits by 1- <br> digit (grouping) | $4 / 5$ | Place value counters <br> Counters | Place value grid <br> Written short division |
| Divide 3-digits by 1- <br> digit (sharing with <br> exchange) | 4 | Base 10 <br> Bar model | Place value counters <br> Part-whole model |
| Divide 3-digits by 1- <br> digit (grouping) | $4 / 5$ | Place value counters <br> Counters | Place value grid <br> Divide 4-digits by 1- <br> digit (grouping) <br> 5Place value counters <br> Counters |
| Divide multi-digits <br> by 2-digits (short <br> division) | 6 | Written short division | Place value grid |
| Divide multi-digits <br> by 2-digits (long <br> division) | 6 | Written long division | List of multiples |

Skill: Solve 1-step problems using multiplication (sharing) $\quad$| Year: $1 / 2$ |
| :--- |

Skill: Solve 1-step problems using division (grouping) $\quad$| Year: $1 / 2$ |
| :--- |

| Tens | Ones |
| :---: | :---: |
| (1)(1) | (1) (1)(1) (1) |
| (1)(1) | (1) (1)(1) (1) |



When dividing larger numbers, children can use manipulatives that allow them to partition into tens and ones.

Straws, Base 10 and


## $48 \div 2=24$

 place value counters can all be used to share numbers into equal groups.

Part-whole models can provide children with a clear written method that matches the concrete representation.



Skill: Divide 2-digits by 1-digit (grouping) $\quad$| Year: 4/5 |
| :--- |
| Tens |


Skill: Divide 3-digits by 1-digit (grouping)
Skill: Divide 4-digits by 1-digit (grouping)




## Glossary

Addend - a number to be added to another.
Aggregation - combining two or more quantities or measures to find a total.
Array - an ordered collection of counters, cubes or other items in rows and columns.
Augmentation - increasing a quantity or measure by another quantity.
Commutative - numbers can be added or multiplied in any order.
Complement - in addition, a number and its complement make a total.
Difference - the numerical difference between two numbers is found by comparing the quantity in each group.

Dividend - in division, the number that is divided.
Divisor - in division, the number by which another is divided.

## Glossary

Exchange - change a number or expression for another of an equal value.
Factor - a number that multiples with another to make a product.
Minuend - a quantity or number from which another is subtracted.
Multiplicand - in multiplication, a number to be multiplied by another.
Partitioning - splitting a number into its component parts.
Product - the result of multiplying one number by another.
Quotient - the result of a division.
Reduction - subtraction as take away.
Remainder - the amount left over after a division when the divisor is not a factor of the dividend.

## Glossary

Scaling - enlarging or reducing a number by a given amount, called the scale factor.
Subitise - instantly recognise the number of objects in a small group without needing to count.

Subtrahend - a number to be subtracted from.
Sum - the result of an addition.
Total - the aggregate or the sum founded by addition.

